

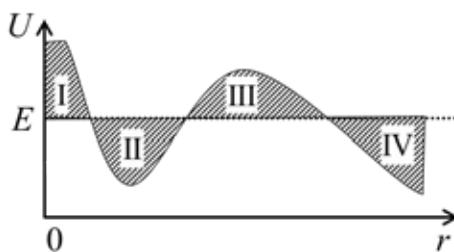
**Paper Specific Instructions**

1. The examination is of 3 hours duration. There are a total of 60 questions carrying 100 marks. The entire paper is divided into three sections, **A**, **B** and **C**. All sections are compulsory. Questions in each section are of different types.
2. **Section – A** contains a total of 30 **Multiple Choice Questions (MCQ)**. Each MCQ type question has four choices out of which only **one** choice is the correct answer. Questions Q.1 – Q.30 belong to this section and carry a total of 50 marks. Q.1 – Q.10 carry 1 mark each and Questions Q.11 – Q.30 carry 2 marks each.
3. **Section – B** contains a total of 10 **Multiple Select Questions (MSQ)**. Each MSQ type question is similar to MCQ but with a difference that there may be **one or more than one** choice(s) that are correct out of the four given choices. The candidate gets full credit if he/she selects all the correct answers only and no wrong answers. Questions Q.31 – Q.40 belong to this section and carry 2 marks each with a total of 20 marks.
4. **Section – C** contains a total of 20 **Numerical Answer Type (NAT)** questions. For these NAT type questions, the answer is a real number which needs to be entered using the virtual keyboard on the monitor. No choices will be shown for these type of questions. Questions Q.41 – Q.60 belong to this section and carry a total of 30 marks. Q.41 – Q.50 carry 1 mark each and Questions Q.51 – Q.60 carry 2 marks each.
5. In all sections, questions not attempted will result in zero mark. In **Section – A** (MCQ), wrong answer will result in **NEGATIVE** marks. For all 1 mark questions, 1/3 marks will be deducted for each wrong answer. For all 2 marks questions, 2/3 marks will be deducted for each wrong answer. In **Section – B** (MSQ), there is **NO NEGATIVE** and **NO PARTIAL** marking provisions. There is **NO NEGATIVE** marking in **Section – C** (NAT) as well.
6. Only Virtual Scientific Calculator is allowed. Charts, graph sheets, tables, cellular phone or other electronic gadgets are **NOT** allowed in the examination hall.
7. The Scribble Pad will be provided for rough work.

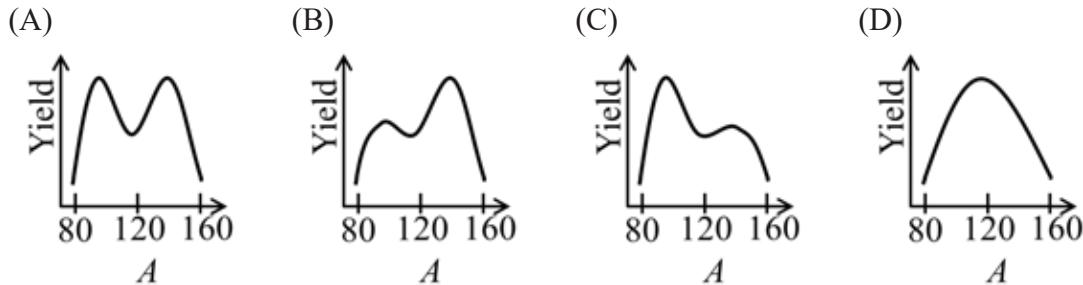
**SECTION – A**  
**MULTIPLE CHOICE QUESTIONS (MCQ)**

**Q. 1 – Q.10 carry one mark each.**

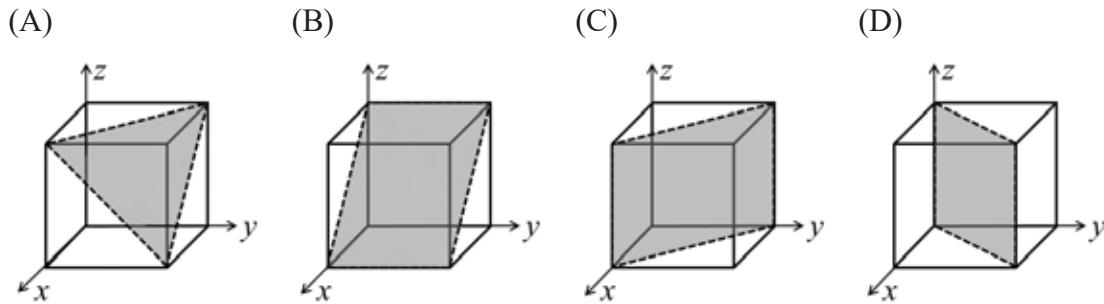
- Q.1 The function  $f(x) \equiv \frac{8x}{x^2 - 9}$  is continuous everywhere except at  
 (A)  $x = 0$       (B)  $x = \pm 3$       (C)  $x = \pm 9i$       (D)  $x = \pm 3i$
- Q.2 A classical particle has total energy  $E$ . The plot of potential energy ( $U$ ) as a function of distance ( $r$ ) from the centre of force located at  $r = 0$  is shown in the figure. Which of the regions are forbidden for the particle?



- (A) I and II      (B) II and IV      (C) I and IV      (D) I and III
- Q.3 In the thermal neutron induced fission of  $^{235}\text{U}$ , the distribution of relative number of the observed fission fragments (Yield) versus mass number ( $A$ ) is given by



- Q.4 Which one of the following crystallographic planes represent (101) Miller indices of a cubic unit cell?



Q.5 The Fermi-Dirac distribution function [ $n(\varepsilon)$ ] is  
( $k_B$  is the Boltzmann constant,  $T$  is the temperature and  $\varepsilon_F$  is the Fermi energy)

(A) $n(\varepsilon) = \frac{1}{e^{\frac{\varepsilon-\varepsilon_F}{k_B T}} - 1}$	(B) $n(\varepsilon) = \frac{1}{e^{\frac{\varepsilon_F-\varepsilon}{k_B T}} - 1}$	(C) $n(\varepsilon) = \frac{1}{e^{\frac{\varepsilon-\varepsilon_F}{k_B T}} + 1}$	(D) $n(\varepsilon) = \frac{1}{e^{\frac{\varepsilon_F-\varepsilon}{k_B T}} + 1}$
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Q.6 If  $\iota(x,y,z)$  is a scalar function which satisfies the Laplace equation, then the gradient of  $\iota$  is

- |                                     |   |
|-------------------------------------|---|
| (A) Solenoidal and irrotational     | (B) Solenoidal but not irrotational     |
| (C) Irrotational but not solenoidal | (D) Neither solenoidal nor irrotational |

Q.7 In a heat engine based on the Carnot cycle, heat is added to the working substance at constant

- |             |              |                 |            |
|-------------|--------------|-----------------|------------|
| (A) Entropy | (B) Pressure | (C) Temperature | (D) Volume |
|-------------|--------------|-----------------|------------|

Q.8 Isothermal compressibility is given by

(A) $\frac{1}{V} \left[ \frac{\partial V}{\partial P} \right]_T$	(B) $\frac{1}{P} \left[ \frac{\partial P}{\partial V} \right]_T$	(C) $0 \frac{1}{V} \left[ \frac{\partial V}{\partial P} \right]_T$	(D) $0 \frac{1}{P} \left[ \frac{\partial P}{\partial V} \right]_T$
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Q.9 For using a transistor as an amplifier, choose the correct option regarding the resistances of base-emitter ( $R_{BE}$ ) and base-collector ( $R_{BC}$ ) junctions

- |  |  |
|--|--|
| (A) Both $R_{BE}$ and $R_{BC}$ are very low  | (B) Very low $R_{BE}$ and very high $R_{BC}$ |
| (C) Very high $R_{BE}$ and very low $R_{BC}$ | (D) Both $R_{BE}$ and $R_{BC}$ are very high |

Q.10 A unit vector perpendicular to the plane containing  $\vec{A} \equiv \hat{i} + 2\hat{k}$  and  $\vec{B} \equiv 2\hat{i} + \hat{j} + \hat{k}$  is

(A) $\frac{1}{\sqrt{26}}(0\hat{i} + 3\hat{j} + 4\hat{k})$	(B) $\frac{1}{\sqrt{19}}(0\hat{i} + 3\hat{j} + 3\hat{k})$
(C) $\frac{1}{\sqrt{35}}(0\hat{i} + 5\hat{j} + 3\hat{k})$	(D) $\frac{1}{\sqrt{35}}(0\hat{i} + 5\hat{j} + 3\hat{k})$

### **Q. 11 – Q. 30 carry two marks each.**

Q.11 A thin lens of refractive index 3/2 is kept inside a liquid of refractive index 4/3. If the focal length of the lens in air is 10 cm, then its focal length inside the liquid is

- |           |           |           |           |
|-----------|-----------|-----------|-----------|
| (A) 10 cm | (B) 30 cm | (C) 40 cm | (D) 50 cm |
|-----------|-----------|-----------|-----------|

Q.12

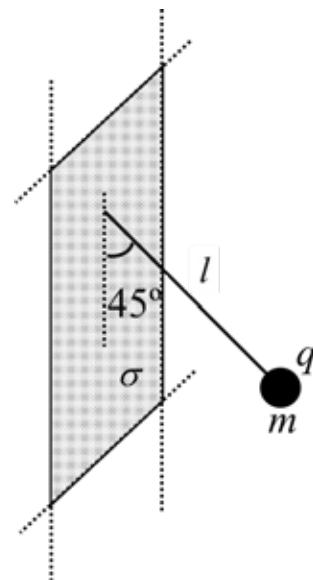
The eigenvalues of  $\begin{bmatrix} 3 & i & 0 \\ 0i & 3 & 0 \\ 0 & 0 & 6 \end{bmatrix}$  are

- (A) 2, 4 and 6      (B)  $2i, 4i$  and 6      (C)  $2i, 4$  and 8      (D) 0, 4 and 8

Q.13 For a quantum particle confined inside a cubic box of side  $L$ , the ground state energy is given by  $E_0$ . The energy of the first excited state is

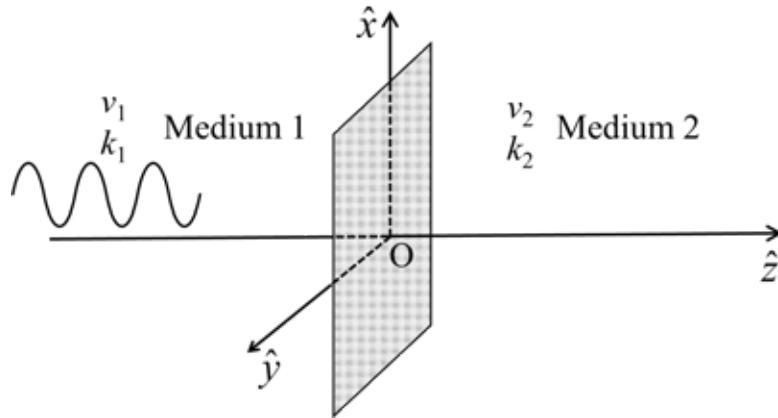
- (A)  $2E_0$       (B)  $\sqrt{2} E_0$       (C)  $3E_0$       (D)  $6E_0$

Q.14 A small spherical ball having charge  $q$  and mass  $m$ , is tied to a thin massless non-conducting string of length  $l$ . The other end of the string is fixed to an infinitely extended thin non-conducting sheet with uniform surface charge density  $\sigma$ . Under equilibrium, the string makes an angle  $45^\circ$  with the sheet as shown in the figure. Then  $\sigma$  is given by ( $g$  is the acceleration due to gravity and  $\eta_0$  is the permittivity of free space)



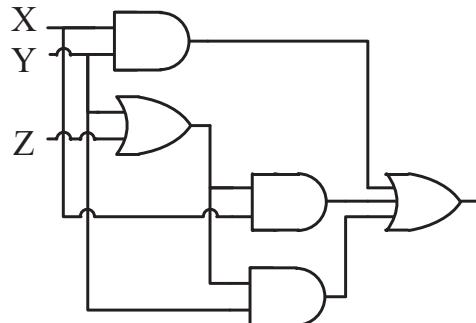
- (A)  $\frac{mg\eta_0}{q}$       (B)  $\sqrt{2} \frac{mg\eta_0}{q}$       (C)  $2 \frac{mg\eta_0}{q}$       (D)  $\frac{mg\eta_0}{q\sqrt{2}}$

- Q.15 Consider the normal incidence of a plane electromagnetic wave with electric field given by  $\vec{E} \equiv E_0 \exp[i(k_1 z_0 \zeta t)] \hat{x}$  over an interface at  $z = 0$  separating two media [wave velocities  $v_1$  and  $v_2$  ( $v_2 > v_1$ ) and wave vectors  $k_1$  and  $k_2$ , respectively] as shown in figure. The magnetic field vector of the reflected wave is ( $\zeta$  is the angular frequency)



- (A)  $\frac{E_0}{v_1} \exp[i(k_1 z_0 \zeta t)] \hat{y}$   
 (B)  $\frac{E_0}{v_1} \exp[i(0k_1 z_0 \zeta t)] \hat{y}$   
 (C)  $\frac{0E_0}{v_1} \exp[i(0k_1 z_0 \zeta t)] \hat{y}$   
 (D)  $\frac{0E_0}{v_1} \exp[i(k_1 z_0 \zeta t)] \hat{y}$

- Q.16 The output of following logic circuit can be simplified to



- (A)  $X + YZ$       (B)  $Y + XZ$       (C)  $XYZ$       (D)  $X + Y + Z$

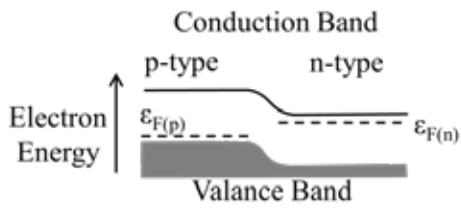
- Q.17 A red star having radius  $r_R$  at a temperature  $T_R$  and a white star having radius  $r_W$  at a temperature  $T_W$ , radiate the same total power. If these stars radiate as perfect black bodies, then

- (A)  $r_R > r_W$  and  $T_R > T_W$       (B)  $r_R < r_W$  and  $T_R > T_W$   
 (C)  $r_R > r_W$  and  $T_R < T_W$       (D)  $r_R < r_W$  and  $T_R < T_W$

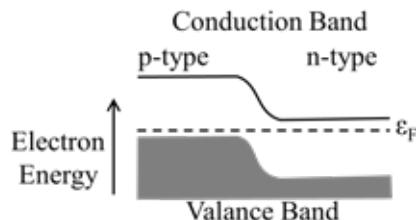
- Q.18 The mass per unit length of a rod (length 2 m) varies as  $\rho = 3x$  kg/m. The moment of inertia (in  $\text{kg m}^2$ ) of the rod about a perpendicular-axis passing through the tip of the rod (at  $x = 0$ ) is  
 (A) 10      (B) 12      (C) 14      (D) 16

- Q.19 For a forward biased p-n junction diode, which one of the following energy-band diagrams is correct?  
( $\epsilon_F$  is the Fermi energy)

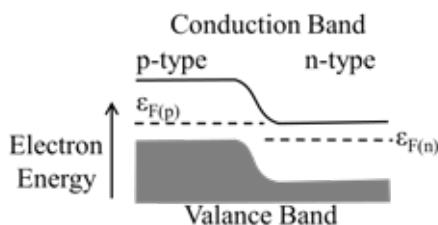
(A)



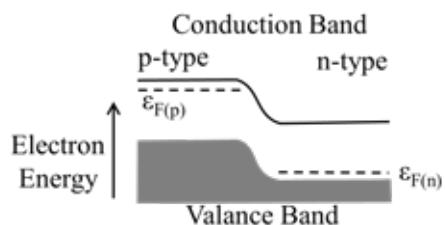
(B)



(C)



(D)



- Q.20 The amount of work done to increase the speed of an electron from  $c/3$  to  $2c/3$  is ( $c = 3 \times 10^8$  m/s and rest mass of electron is 0.511 MeV)

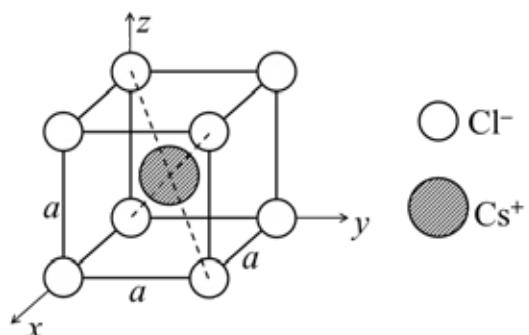
(A) 56.50 keV

(B) 143.58 keV

(C) 168.20 keV

(D) 511.00 keV

- Q.21 The location of  $\text{Cs}^+$  and  $\text{Cl}^-$  ions inside the unit cell of  $\text{CsCl}$  crystal is shown in the figure. The Bravais lattice of  $\text{CsCl}$  is



(A) simple cubic

(B) body centered orthorhombic

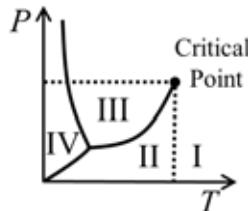
(C) face centered cubic

(D) base centered orthorhombic

- Q.22 A  $\gamma$ -ray photon emitted from a  $^{137}\text{Cs}$  source collides with an electron at rest. If the Compton shift of the photon is  $3.25 \times 10^{-13}$  m, then the scattering angle is closest to (Planck's constant  $h = 6.626 \times 10^{-34}$  J s, electron mass  $m_e = 9.109 \times 10^{-31}$  kg and velocity of light in free space  $c = 3 \times 10^8$  m/s)

(A)  $45^\circ$ (B)  $60^\circ$ (C)  $30^\circ$ (D)  $90^\circ$

- Q.24 In the given phase diagram for a pure substance, regions I, II, III, IV, respectively represent



- (A) Vapor, Gas, Solid, Liquid      (B) Gas, Vapor, Liquid, Solid  
(C) Gas, Liquid, Vapor, Solid      (D) Vapor, Gas, Liquid, Solid

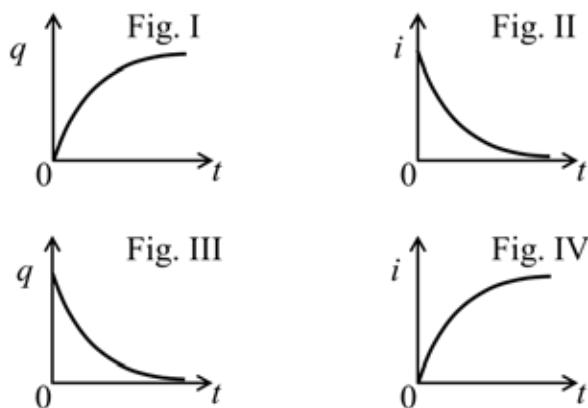
- Q.25 Light of wavelength  $\lambda$  (in free space) propagates through a dispersive medium with refractive index  $n(\lambda)=1.5 + 0.6\lambda$ . The group velocity of a wave travelling inside this medium in units of  $10^8$  m/s is



- Q.26** The maximum number of intensity minima that can be observed in the Fraunhofer diffraction pattern of a single slit (width 10  $\mu\text{m}$ ) illuminated by a laser beam (wavelength 0.630  $\mu\text{m}$ ) will be



- Q.27 During the charging of a capacitor  $C$  in a series RC circuit, the typical variations in the magnitude of the charge  $q(t)$  deposited on one of the capacitor plates, and the current  $i(t)$  in the circuit, respectively are best represented by



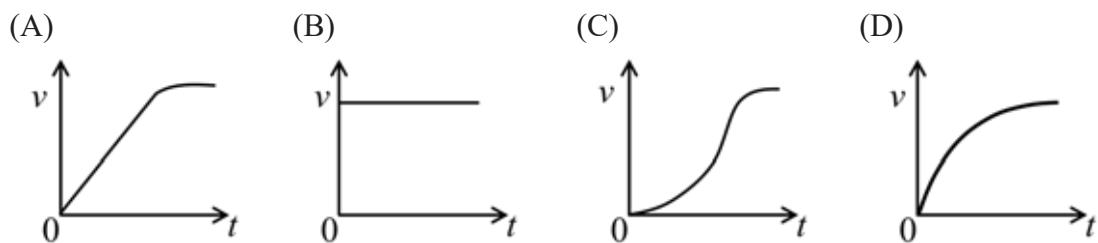
Q.28 Which one of the following is an impossible magnetic field  $\vec{B}$ ?

- (A)  $\vec{B} \approx 3x^2z^2\hat{x} + 2xz^3\hat{z}$
- (B)  $\vec{B} \approx 02xy\hat{x} + yz^2\hat{y} + \left[ 2yz + \frac{z^3}{3} \right]\hat{z}$
- (C)  $\vec{B} \approx +xz + 4y\hat{x} + yx^3\hat{y} + \left[ x^3z + \frac{z^2}{2} \right]\hat{z}$
- (D)  $\vec{B} \approx 06xz\hat{x} + 3yz^2\hat{y}$

Q.29 If the motion of a particle is described by  $x = 5 \cos(8\pi t)$ ,  $y = 5 \sin(8\pi t)$  and  $z = 5t$ , then the trajectory of the particle is

- (A) Circular
- (B) Elliptical
- (C) Helical
- (D) Spiral

Q.30 A ball of mass  $m$  is falling freely under gravity through a viscous medium in which the drag force is proportional to the instantaneous velocity  $v$  of the ball. Neglecting the buoyancy force of the medium, which one of the following figures best describes the variation of  $v$  as a function of time  $t$ ?



## SECTION - B

### MULTIPLE SELECT QUESTIONS (MSQ)

**Q. 31 – Q. 40 carry two marks each.**

Q.31 The relation between the nuclear radius ( $R$ ) and the mass number ( $A$ ), given by  $R = 1.2 A^{1/3}$  fm, implies that

- (A) The central density of nuclei is independent of  $A$
- (B) The volume energy per nucleon is a constant
- (C) The attractive part of the nuclear force has a long range
- (D) The nuclear force is charge dependent

Q.32 Consider an object moving with a velocity  $\vec{v}$  in a frame which rotates with a constant angular velocity  $\vec{\omega}$ . The Coriolis force experienced by the object is

- (A) along  $\vec{v}$
- (B) along  $\vec{\omega}$
- (C) perpendicular to both  $\vec{v}$  and  $\vec{\omega}$
- (D) always directed towards the axis of rotation

Q.33 The gradient of a scalar field  $S(x,y,z)$  has the following characteristic(s).

- (A) Line integral of a gradient is path-independent
- (B) Closed line integral of a gradient is zero
- (C) Gradient of  $S$  is a measure of the maximum rate of change in the field  $S$
- (D) Gradient of  $S$  is a scalar quantity

Q.34 A thermodynamic system is described by the  $P, V, T$  coordinates. Choose the valid expression(s) for the system.

$$\begin{array}{ll} \text{(A)} \left[ \frac{\partial P}{\partial V} \right]_T \left[ \frac{\partial V}{\partial T} \right]_P \equiv 0 & \text{(B)} \left[ \frac{\partial P}{\partial V} \right]_T \left[ \frac{\partial V}{\partial T} \right]_P \equiv \left[ \frac{\partial P}{\partial T} \right]_V \\ \text{(C)} \left[ \frac{\partial V}{\partial T} \right]_P \left[ \frac{\partial T}{\partial P} \right]_V \equiv 0 & \text{(D)} \left[ \frac{\partial V}{\partial T} \right]_P \left[ \frac{\partial T}{\partial P} \right]_V \equiv \left[ \frac{\partial V}{\partial P} \right]_T \end{array}$$

Q.35 Which of the following statement(s) is/are true?

- (A) Newton's laws of motion and Maxwell's equations are both invariant under Lorentz transformations.
- (B) Newton's laws of motion and Maxwell's equations are both invariant under Galilean transformations.
- (C) Newton's laws of motion are invariant under Galilean transformations and Maxwell's equations are invariant under Lorentz transformations.
- (D) Newton's laws of motion are invariant under Lorentz transformations and Maxwell's equations are invariant under Galilean transformations.

Q.36 For an underdamped harmonic oscillator with velocity  $v(t)$ ,

- (A) Rate of energy dissipation varies linearly with  $v(t)$
- (B) Rate of energy dissipation varies as square of  $v(t)$
- (C) The reduction in the oscillator frequency, compared to the undamped case, is independent of  $v(t)$
- (D) For weak damping, the amplitude decays exponentially to zero

Q.37 Out of the following statements, choose the correct option(s) about a perfect conductor.

- (A) The conductor has an equipotential surface
- (B) Net charge, if any, resides only on the surface of conductor
- (C) Electric field cannot exist inside the conductor
- (D) Just outside the conductor, the electric field is always perpendicular to its surface

Q.38 In the X-ray diffraction pattern recorded for a simple cubic solid (lattice parameter  $a = 1 \text{ \AA}$ ) using X rays of wavelength  $1 \text{ \AA}$ , the first order diffraction peak(s) would appear for the

- |                  |                  |
|------------------|------------------|
| (A) (100) planes | (B) (112) planes |
| (C) (210) planes | (D) (220) planes |

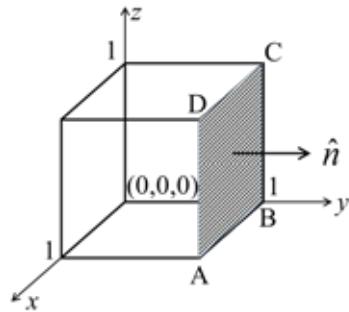
- Q.39 Consider a classical particle subjected to an attractive inverse-square force field. The total energy of the particle is E and the eccentricity is  $\varepsilon$ . The particle will follow a parabolic orbit if
- (A)  $E > 0$  and  $\varepsilon = 1$       (B)  $E < 0$  and  $\varepsilon < 1$   
 (C)  $E = 0$  and  $\varepsilon = 1$       (D)  $E < 0$  and  $\varepsilon = 1$
- Q.40 An atomic nucleus X with half-life  $T_X$  decays to a nucleus Y, which has half-life  $T_Y$ . The condition(s) for secular equilibrium is(are)
- (A)  $T_X \approx T_Y$       (B)  $T_X < T_Y$       (C)  $T_X \ll T_Y$       (D)  $T_X \gg T_Y$

**SECTION – C**  
**NUMERICAL ANSWER TYPE (NAT)**

**Q. 41 – Q. 50 carry one mark each.**

- Q.41 In a typical human body, the amount of radioactive  $^{40}\text{K}$  is  $3.24 \times 10^{-5}$  percent of its mass. The activity due to  $^{40}\text{K}$  in a human body of mass 70 kg is \_\_\_\_\_ kBq.  
 (Round off to 2 decimal places)  
 (Half-life of  $^{40}\text{K} = 3.942 \times 10^{16}$  s, Avogadro's number  $N_A = 6.022 \times 10^{23}$  mol $^{-1}$ )
- Q.42 Sodium (Na) exhibits body-centered-cubic (BCC) crystal structure with atomic radius 0.186 nm. The lattice parameter of Na unit cell is \_\_\_\_\_ nm.  
 (Round off to 2 decimal places)
- Q.43 Light of wavelength 680 nm is incident normally on a diffraction grating having 4000 lines/cm. The diffraction angle (in degrees) corresponding to the third-order maximum is \_\_\_\_\_.  
 (Round off to 2 decimal places)
- Q.44 Two gases having molecular diameters  $D_1$  and  $D_2$ , and mean free paths  $\sigma_1$  and  $\sigma_2$ , respectively, are trapped separately in identical containers.  
 If  $D_2 = 2D_1$ , then  $\sigma_1/\sigma_2 =$  \_\_\_\_\_.  
 (Assume there is no change in other thermodynamic parameters)
- Q.45 An object of 2 cm height is placed at a distance of 30 cm in front of a concave mirror with radius of curvature 40 cm. The height of the image is \_\_\_\_\_ cm.

- Q.46 The flux of the function  $\vec{F} \equiv (y^2)\hat{x} + (3xy + z^2)\hat{y} + (4yz)\hat{z}$  passing through the surface ABCD along  $\hat{n}$  is \_\_\_\_\_.  
(Round off to 2 decimal places)

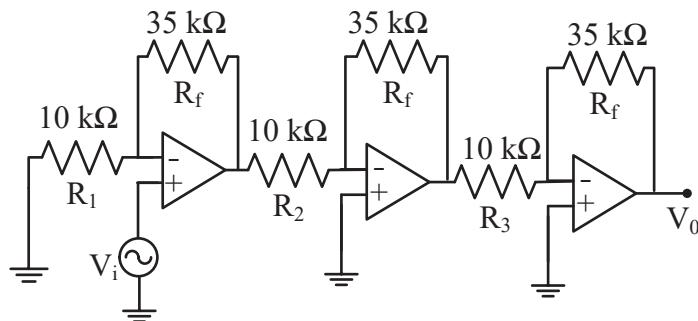


- Q.47 The electrostatic energy (in units of  $\frac{1}{4\sigma\eta_0}$  J) of a uniformly charged spherical shell of total charge 5 C and radius 4 m is \_\_\_\_\_.  
(Round off to 3 decimal places)

- Q.48 An infinitely long very thin straight wire carries uniform line charge density  $8\pi \times 10^{-2}$  C/m. The magnitude of electric displacement vector at a point located 20 mm away from the axis of the wire is \_\_\_\_ C/m<sup>2</sup>.

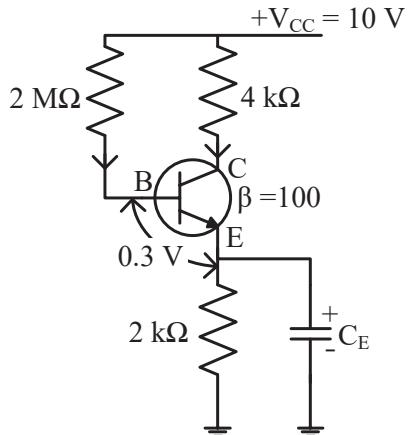
- Q.49 The 7<sup>th</sup> bright fringe in the Young's double slit experiment using a light of wavelength 550 nm shifts to the central maxima after covering the two slits with two sheets of different refractive indices  $n_1$  and  $n_2$  but having same thickness 6  $\mu\text{m}$ . The value of  $|n_1 - n_2|$  is \_\_\_\_\_.  
(Round off to 2 decimal places)

- Q.50 For the input voltage  $V_i = (200 \text{ mV}) \sin(400t)$ , the amplitude of the output voltage ( $V_0$ ) of the given OPAMP circuit is \_\_\_\_ V.  
(Round off to 2 decimal places)



**Q. 51 – Q. 60 carry two marks each.**

- Q.51 The value of emitter current in the given circuit is \_\_\_\_\_  $\mu\text{A}$ .  
 (Round off to 1 decimal place)



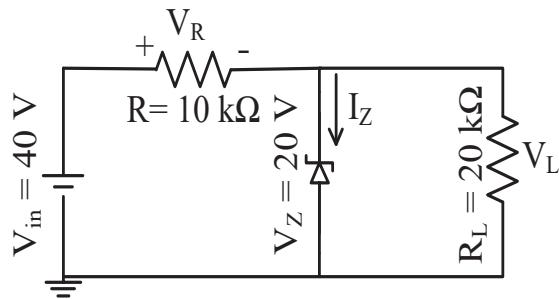
- Q.52 The value of  $\left| \int_0^{3y} +z^2 dz \right|^2$ , along the line  $3y \equiv x$ , where  $z \equiv x$ .  $i_y$  is \_\_\_\_\_.  
 (Round off to 1 decimal place)

- Q.53 If the wavelength of  $K\alpha_2$  X-ray line of an element is  $1.544\text{\AA}$ , then the atomic number ( $Z$ ) of the element is \_\_\_\_\_.  
 (Rydberg constant  $R = 1.097 \times 10^7 \text{ m}^{-1}$  and velocity of light  $c = 3 \times 10^8 \text{ m/s}$ )

- Q.54 A proton is confined within a nucleus of size  $10^{-13} \text{ cm}$ . The uncertainty in its velocity is  $\frac{1}{\sqrt{m_p}} \times 10^8 \text{ m/s}$ .  
 (Round off to 2 decimal places)  
 (Planck's constant  $h = 6.626 \times 10^{-34} \text{ J s}$  and proton mass  $m_p = 1.672 \times 10^{-27} \text{ kg}$ )

- Q.55 Given the wave function of a particle /  $(x) \equiv \sqrt{\frac{2}{L}} \sin\left(\frac{\sigma}{L}x\right)$  for  $0 < x < L$  and 0 elsewhere,  
 the probability of finding the particle between  $x = 0$  and  $x = L/2$  is \_\_\_\_\_.  
 (Round off to 1 decimal place)

Q.56 The Zener current  $I_Z$  for the given circuit is \_\_\_\_\_ mA.



Q.57 If the diameter of the Earth is increased by 4% without changing the mass, then the length of the day is \_\_\_\_\_ hours.

(Take the length of the day before the increment as 24 hours. Assume the Earth to be a sphere with uniform density.)

(Round off to 2 decimal places)

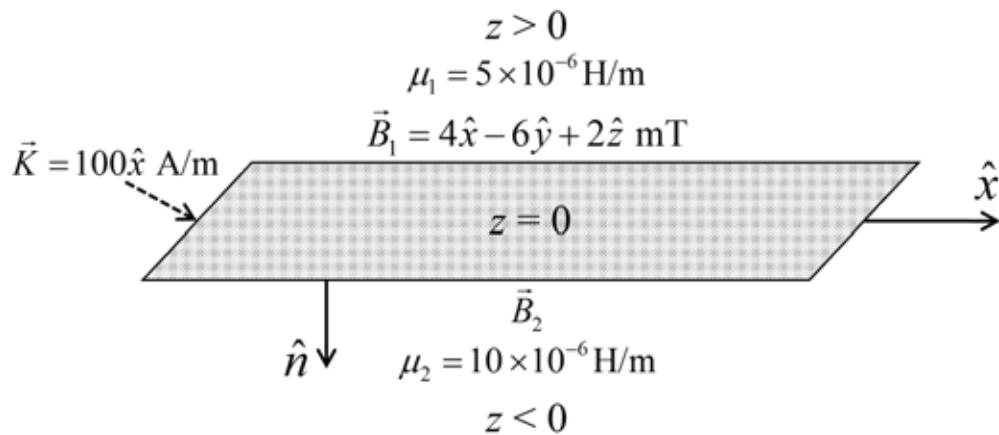
Q.58 A di-atomic gas undergoes adiabatic expansion against the piston of a cylinder. As a result, the temperature of the gas drops from 1150 K to 400 K. The number of moles of the gas required to obtain 2300 J of work from the expansion is \_\_\_\_\_.

(The gas constant  $R = 8.314 \text{ J mol}^{-1}\text{K}^{-1}$ .)

(Round off to 2 decimal places)

Q.59 The decimal equivalent of the binary number 110.101 is \_\_\_\_\_.

Q.60 A surface current  $\vec{K} \equiv 100 \hat{x} \text{ A/m}$  flows on the surface  $z = 0$ , which separates two media with magnetic permeabilities  $\mu_1$  and  $\mu_2$  as shown in the figure. If the magnetic field in the region 1 is  $\vec{B}_1 = 4\hat{x} - 6\hat{y} + 2\hat{z} \text{ mT}$ , then the magnitude of the normal component of  $\vec{B}_2$  will be \_\_\_\_\_ mT.



**END OF THE QUESTION PAPER**